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Linearly Polarized Gluons and the Higgs Transverse Momentum Distribution

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We study how gluons carrying linear polarization inside an unpolarized hadron contribute to the transverse momentum distribution of Higgs bosons produced in hadronic collisions. They modify the distribution produced by unpolarized gluons in a characteristic way that could be used to determine whether the Higgs boson is a scalar or a pseudoscalar particle.

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It is sometimes said that the LHC is a “gluon collider,” because at high energies the gluon density inside a proton becomes dominant over the quark densities. Higgs boson production, in particular, predominantly arises from gluon-gluon “fusion” $gg \rightarrow H$ through a triangular top quark loop. QCD corrections to this process have been calculated with increasing precision [1–7], making it well understood. It is not commonly known, however, that the LHC is actually also to some extent a *polarized* gluon collider, since gluons can, in principle, be linearly polarized inside an unpolarized proton. Their corresponding distribution, here denoted by $h_1^{\perp g}$ and first defined in Ref. [8], requires the gluons to have a nonzero transverse momentum with respect to the parent hadron. It corresponds to an interference between $+1$ and -1 helicity gluon states that would be suppressed without transverse momentum.

So far, the function $h_1^{\perp g}$ has not been studied experimentally, and consequently nothing is known about its magnitude. Only a theoretical upper bound has been given [8,9]. Recently, several ways of probing $h_1^{\perp g}$ have been put forward, namely, in heavy quark pair or dijet production [9] or in photon pair production [10], where in all cases the transverse momentum of the pair is measured. One way in which linearly polarized gluons can manifest themselves in these processes is through azimuthal asymmetries. However, it was found that they can also generate a term in the cross section that is independent of the azimuthal angle. This happens when two linearly polarized gluons, one from each hadron, participate in the scattering. In this way, they can also contribute to production of a scalar particle, such as a scalar or pseudoscalar Higgs boson, when its transverse momentum q_T is measured. It has, in fact, been shown [11,12] that such a contribution is generated perturbatively. In other words, if at tree level gluons are taken to be unpolarized, at order α_s they will become to some extent linearly polarized. In the transverse momentum distribution of spin-0 particles produced in proton-proton collisions, this will give rise to an additional contribution at order α_s^2 , because of the double helicity flip

involved (see Fig. 1). While this may be expected to make only a relatively modest contribution, the function $h_1^{\perp g}$ is of *nonperturbative* nature and is present at tree level already. Therefore, a significant influence of linearly polarized gluons on the distribution of the produced particle at low q_T is not excluded.

In light of this, we will investigate in this Letter how the distribution of linearly polarized gluons may affect the transverse momentum distribution of Higgs bosons for $q_T \ll m_H$, where m_H is the Higgs boson mass. We shall observe that linearly polarized gluons may, in fact, provide a tool to uncover whether the Higgs boson is a scalar or a pseudoscalar particle. Thus far, relatively few suggestions to this end have been put forward for the LHC, typically by using azimuthal distributions, for example, in Higgs + jet pair production [13] or in τ pair decays [14]. The suggestion we put forward here does not involve measurements of any angular distributions. Instead, we will show that linear polarization of gluons simply leads to a modulation of the Higgs transverse momentum distribution that depends on the nature of the Higgs particle.

Transverse momentum dependent distribution functions (TMDs) of gluons in an unpolarized hadron are defined through a matrix element of a correlator of the gluon field strengths $F^{\mu\nu}(0)$ and $F^{\nu\sigma}(\xi)$, evaluated at fixed light-front (LF) time $\xi^+ = \xi \cdot n = 0$, where n is a lightlike vector

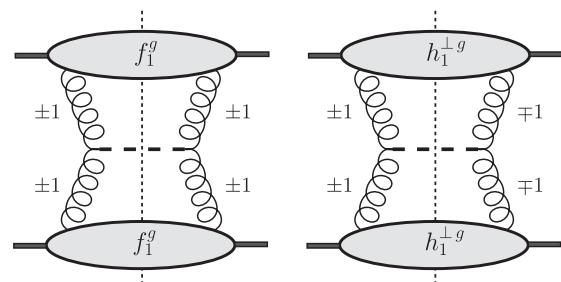


FIG. 1. Gluon helicities in the $gg \rightarrow H$ squared amplitude for unpolarized (left) and linearly polarized production (right).

conjugate to the parent hadron's four-momentum P . By decomposing the gluon momentum as $p = xP + p_T + p^-n$, the correlator is given by [8]

$$\begin{aligned}\Phi_g^{\mu\nu}(x, \mathbf{p}_T) &= \frac{n_\rho n_\sigma}{(p \cdot n)^2} \int \frac{d(\xi \cdot P) d^2 \xi_T}{(2\pi)^3} e^{ip \cdot \xi} \\ &\times \langle P | \text{Tr}[F^{\mu\rho}(0) F^{\nu\sigma}(\xi)] | P \rangle_{\text{LF}} \\ &= -\frac{1}{2x} \left\{ g_T^{\mu\nu} f_1^g - \left(\frac{p_T^\mu p_T^\nu}{M^2} + g_T^{\mu\nu} \frac{p_T^2}{2M^2} \right) h_1^{\perp g} \right\},\end{aligned}\quad (1)$$

with $p_T^2 = -\mathbf{p}_T^2$, $g_T^{\mu\nu} = g^{\mu\nu} - P^\mu n^\nu / P \cdot n - n^\mu P^\nu / P \cdot n$, and M the proton mass. $f_1^g(x, \mathbf{p}_T^2)$ represents the unpolarized gluon distribution and $h_1^{\perp g}(x, \mathbf{p}_T^2)$ the distribution of linearly polarized gluons. In Eq. (1), we have omitted a Wilson line that renders the correlator gauge invariant. As any TMD, $h_1^{\perp g}$ will receive contributions from initial and/or final state interactions, which make the gauge link process-dependent. Therefore, despite the fact that it is T -even, $h_1^{\perp g}$ can receive nonuniversal contributions, and its extraction can be hampered for processes where factorization does not hold, such as dijet production in hadron-hadron collisions [15–17]. Higgs boson production, on the other hand, is expected to allow for TMD factorization, just like the Drell-Yan process. A more detailed study of this remains to be carried out.

The calculation of the Higgs boson production cross section in the TMD framework closely follows Refs. [15,18]. The generic contribution by $gg \rightarrow H$ reads

$$\begin{aligned}E_H \frac{d\sigma}{d^3 \vec{q}} \Big|_{q_T \ll m_H} &= \frac{\pi x_a x_b}{16m_H^2 S} \int d^2 \mathbf{p}_{aT} \int d^2 \mathbf{p}_{bT} \\ &\times \delta^2(\mathbf{p}_{aT} + \mathbf{p}_{bT} - \mathbf{q}_T) \Phi_g^{\mu\nu}(x_a, \mathbf{p}_{aT}) \\ &\times \Phi_g^{\rho\sigma}(x_b, \mathbf{p}_{bT}) (\hat{\mathcal{M}}^{\mu\rho}) (\hat{\mathcal{M}}^{\nu\sigma})^* \Big|_{p_b=x_b P_b}^{p_b=x_b P_b} \\ &+ \mathcal{O}\left(\frac{q_T}{m_H}\right).\end{aligned}\quad (2)$$

For now, we assume on-shell production of the Higgs particle, with \vec{q} and E_H its momentum and energy. P_a and P_b are the momenta of the colliding protons, $S = (P_a + P_b)^2$, and $x_{a(b)} = q^2/(2P_{a(b)} \cdot q)$. To lowest order, the hard partonic amplitude $\hat{\mathcal{M}}$ is given by the well-known formula [4] for the $gg \rightarrow H$ triangle diagram:

$$\hat{\mathcal{M}}_H^{\mu\nu} = i2^{1/4} G_F^{1/2} \alpha_s m_H^2 g_T^{\mu\nu} \mathcal{A}_H(\tau)/(8\pi) \quad (3)$$

for a scalar standard model (SM) Higgs boson H^0 , where we consider only top quarks in the triangle and where G_F is the Fermi constant, α_s the strong coupling constant, $\tau = m_H^2/(4m_t^2)$ with the top mass m_t , and $\mathcal{A}_H(\tau) = 2[\tau + (\tau - 1)J(\tau)]/\tau^2$ with

$$J(\tau) = \begin{cases} -\frac{1}{4} \left[\ln\left(\frac{1+\sqrt{1-1/\tau}}{1-\sqrt{1-1/\tau}}\right) - i\pi \right]^2, & \tau > 1, \\ \arcsin^2(\sqrt{\tau}), & \tau \leq 1. \end{cases} \quad (4)$$

For a pseudoscalar Higgs boson A^0 with a simple coupling $g_t(\sqrt{2}G_F)^{1/2}m_t^2\gamma_5$ to quarks [19], we have instead

$$\hat{\mathcal{M}}_A^{\mu\nu} = i2^{1/4} G_F^{1/2} \alpha_s m_H^2 \epsilon_T^{\mu\nu} \mathcal{A}_A(\tau)/(8\pi), \quad (5)$$

where $\epsilon_T^{\mu\nu}$ is the two-dimensional Levi-Civita tensor and $\mathcal{A}_A(\tau) = g_t 2J(\tau)/\tau$. As mentioned above, QCD corrections to these amplitudes have been calculated. However, since our goal is to study the effect of linearly polarized gluons whose distribution $h_1^{\perp g}$ is anyway unknown, we limit ourselves to the lowest-order expressions (3) and (5). This leads to the following expressions for scalar and pseudoscalar Higgs boson production:

$$\begin{aligned}E_H \frac{d\sigma^{H(A)}}{d^3 \vec{q}} \Big|_{q_T \ll m_H} &= \frac{\pi\sqrt{2}G_F}{128m_H^2 S} \left(\frac{\alpha_s}{4\pi} \right)^2 |\mathcal{A}_{H(A)}(\tau)|^2 (\mathcal{C}[f_1^g f_1^g] \\ &\pm \mathcal{C}[w_H h_1^{\perp g} h_1^{\perp g}]) + \mathcal{O}\left(\frac{q_T}{m_H}\right),\end{aligned}\quad (6)$$

where the upper (lower) sign refers to the scalar (pseudoscalar) case and where we have the TMD convolution

$$\begin{aligned}\mathcal{C}[wff] &\equiv \int d^2 \mathbf{p}_{aT} \int d^2 \mathbf{p}_{bT} \delta^2(\mathbf{p}_{aT} + \mathbf{p}_{bT} - \mathbf{q}_T) \\ &\times w(\mathbf{p}_{aT}, \mathbf{p}_{bT}) f(x_a, \mathbf{p}_{aT}^2) f(x_b, \mathbf{p}_{bT}^2),\end{aligned}\quad (7)$$

with the transverse momentum weight

$$w_H = \frac{(\mathbf{p}_{aT} \cdot \mathbf{p}_{bT})^2 - \frac{1}{2} \mathbf{p}_{aT}^2 \mathbf{p}_{bT}^2}{2M^4}. \quad (8)$$

We emphasize the sign difference in the $\mathcal{C}[w_H h_1^{\perp g} h_1^{\perp g}]$ term in Eq. (6), which may offer an opportunity to determine the parity of the Higgs boson. The terms involving $h_1^{\perp g}$ have the model-independent property $\langle q_T^2 \rangle_{hh} \equiv \int d^2 \mathbf{q}_T (\mathbf{q}_T^2)^\alpha \mathcal{C}[w_H h_1^{\perp g} h_1^{\perp g}] = 0$ for $\alpha = 0, 1$. This feature points towards a distinctive transverse momentum distribution of the $h_1^{\perp g} h_1^{\perp g}$ term with a double node in \mathbf{q}_T . We note that, since $\langle 1 \rangle_{hh} = 0$, linearly polarized gluons do not affect the \mathbf{q}_T -integrated cross section.

In the following, we estimate the possible size of the contribution by linearly polarized gluons to the Higgs boson production cross section at tree level. Although the function $h_1^{\perp g}$ itself is unknown, a model-independent positivity bound for it has been derived in Ref. [8]:

$$\frac{\mathbf{p}_T^2}{2M^2} |h_1^{\perp g}(x, \mathbf{p}_T^2)| \leq f_1^g(x, \mathbf{p}_T^2), \quad (9)$$

valid for all x and \mathbf{p}_T . The maximally possible effect will be generated when this bound is saturated. Models may also shed light on the size of $h_1^{\perp g}$. In the simple perturbative quark target model of gluon TMDs of Ref. [20], the

function $h_1^{\perp g}$ is found to possess the same characteristic $1/x$ increase as the distribution of unpolarized gluons f_1^g , which suggests that linearly polarized gluons may be as relevant at small x as unpolarized ones. Another recent model calculation [21] shows saturation of the positivity bound for $h_1^{\perp g}$ in heavy nuclei in certain transverse momentum regions (Weizsäcker-Williams model) or even over the full momentum range (dipole model). This suggests that saturation of the positivity bound at least locally in x or p_T^2 might not be an unrealistic assumption.

We follow a standard approach for TMDs in the literature (see [22]) and assume a simple Gaussian dependence of the gluon TMDs on transverse momentum:

$$f_1^g(x, p_T^2) = \frac{G(x)}{\pi \langle p_T^2 \rangle} \exp\left(-\frac{p_T^2}{\langle p_T^2 \rangle}\right), \quad (10)$$

where $G(x)$ is the collinear gluon distribution and the width $\langle p_T^2 \rangle$ is assumed to be independent of x . The bound (9) is directly satisfied by the form

$$h_1^{\perp g}(x, p_T^2) = \frac{M^2 G(x)}{\pi \langle p_T^2 \rangle^2} \frac{2e(1-r)}{r} \exp\left(-\frac{p_T^2}{r \langle p_T^2 \rangle}\right). \quad (11)$$

We choose $r = 2/3$. The left panel of Fig. 2 shows the p_T dependence of f_1^g and $h_1^{\perp g}$ for two values of the Gaussian width: $\langle p_T^2 \rangle = 1 \text{ GeV}^2$ and $\langle p_T^2 \rangle = 7 \text{ GeV}^2$. The latter value may be more appropriate at $Q = m_H$; cf. the Gaussian fit to $f_1^u(x, p_T^2)$ evolved to $Q = M_Z$ of Ref. [23].

It is straightforward to compute the convolution integrals appearing in Eq. (6) analytically:

$$\mathcal{C}[f_1^g f_1^g] = \frac{G(x_a)G(x_b)}{2\pi \langle p_T^2 \rangle} \exp\left(-\frac{q_T^2}{2 \langle p_T^2 \rangle}\right), \quad (12)$$

$$\begin{aligned} \mathcal{C}[w_H h_1^{\perp g} h_1^{\perp g}] &= \frac{G(x_a)G(x_b)}{36\pi \langle p_T^2 \rangle} \left[\frac{2}{3} - \frac{q_T^2}{\langle p_T^2 \rangle} + \frac{3(q_T^2)^2}{16 \langle p_T^2 \rangle^2} \right] \\ &\times \exp\left(2 - \frac{3q_T^2}{4 \langle p_T^2 \rangle}\right). \end{aligned} \quad (13)$$

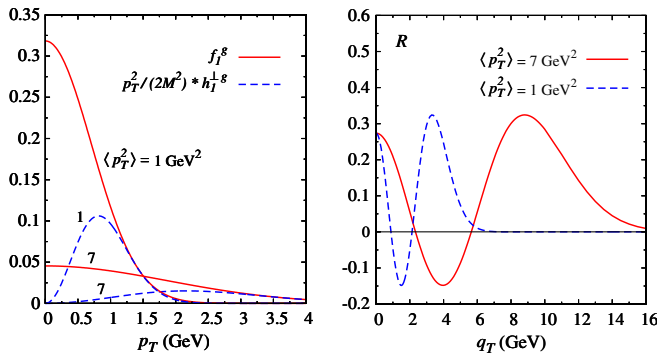


FIG. 2 (color online). Left: Gaussian distributions for f_1^g and $h_1^{\perp g}$ [divided by $G(x)$] as functions of p_T for two different values of $\langle p_T^2 \rangle$. Right: Resulting ratio $R = \mathcal{C}[w_H h_1^{\perp g} h_1^{\perp g}] / \mathcal{C}[f_1^g f_1^g]$.

Their ratio R is shown in the right panel of Fig. 2. It is a measure of the relative size of the contribution by linearly polarized gluons and shows the anticipated double node of $\mathcal{C}[w_H h_1^{\perp g} h_1^{\perp g}]$. It is evident that, at least within our simple model, linearly polarized gluons have a sizable effect on the Higgs q_T distribution. We stress again that the effect enters scalar and pseudoscalar Higgs boson production with opposite sign. If the effect is at or near the level shown by Fig. 2, it should easily allow us to determine the parity of the Higgs boson, provided a sufficiently fine scan in q_T is possible in experiment, to resolve both nodes.

So far, we have considered only the production of an on-shell Higgs boson. In reality, the Higgs boson will decay into some observed final state, and there will be background reactions contributing to this final state that are not related to the Higgs boson. These backgrounds may themselves be sensitive to linearly polarized gluons. We will now briefly consider one example of this, the Higgs boson decay into a photon pair. We reserve a more detailed study of final states such as γZ , ZZ , or WW for a future publication.

After production in $gg \rightarrow H$, the two-photon decay of a SM Higgs boson occurs through a top quark or W -boson triangular loop. The decay of a pseudoscalar Higgs boson is instead described by physics beyond the SM and hence is model-dependent. There are often no tree-level couplings to W bosons in this case [24], so here we consider only the top quark coupling. For both a scalar or pseudoscalar Higgs boson, the lowest-order amplitude can be written as [25]

$$\hat{\mathcal{M}}_{\gamma\gamma}^{\mu\nu} = \frac{\sqrt{2}G_F \alpha_s \alpha}{32\pi^2} \frac{s^2 \mathcal{A}_{H(A)}(\bar{\tau}) \mathcal{F}_{H(A) \rightarrow \gamma\gamma}(s)}{s - m_H^2 + i\Gamma_H m_H} r^{\mu\nu}, \quad (14)$$

where α is the electromagnetic coupling and Γ_H the Higgs boson decay width. For a scalar Higgs boson, $r^{\mu\nu} = g_T^{\mu\nu} \delta_{\lambda_a \lambda_b}$, whereas $r^{\mu\nu} = \lambda_a i \epsilon_T^{\mu\nu} \delta_{\lambda_a \lambda_b}$ in the pseudoscalar case, with λ_a and λ_b the photon helicities. $\mathcal{A}_H(\bar{\tau})$ and $\mathcal{A}_A(\bar{\tau})$ are given in Eqs. (3) and (5) with $\bar{\tau} = s/(4m_t^2)$, where $s = (p_a + p_b)^2 \simeq x_a x_b S$ for gluon momenta p_a and p_b . Finally,

$$\mathcal{F}_{H \rightarrow \gamma\gamma}(s) = \mathcal{W}(\tau_W) + \frac{4}{9} N_c \mathcal{A}_H(\bar{\tau}), \quad (15)$$

with $\tau_W = s/(4m_W^2)$ and $\mathcal{W}(\tau) = -[2\tau^2 + 3\tau + 3(2\tau - 1)J(\tau)]/\tau^2$ describes the contribution by the W triangular loop. We assume $\mathcal{F}_{A \rightarrow \gamma\gamma}(s) = \frac{4}{9} N_c \mathcal{A}_A(\bar{\tau})$. In the following, we consider a relatively light Higgs boson mass $m_H = 120 \text{ GeV}$ with a small total width $\Gamma_H \simeq 5 \times 10^{-3} \text{ GeV}$ [26].

As is well known, an important QCD background to photon pair production at high energies is generated by $gg \rightarrow \gamma\gamma$ via a quark box [27]. This subprocess was studied recently in the context of TMD factorization in Ref. [10]. Using its results, we add the two lowest-order amplitudes describing the box diagram and the Higgs

resonance and extract the azimuthal-angle independent cross section:

$$\int d\phi \frac{d\sigma^{gg}}{d^4q d\Omega} = F_1 \mathcal{C}[f_1^g f_1^g] + F_2 \mathcal{C}[w_H h_1^{\perp g} h_1^{\perp g}]. \quad (16)$$

Here $q = q_a + q_b$ is the momentum of the photon pair. $d\Omega = d\phi d\cos\theta$ denotes the solid angle element for each photon, with the angles ϕ and θ defined in the Collins-Soper frame [10]. F_1 and F_2 are calculated functions of θ and the pair mass $Q = \sqrt{s}$ that we will not give here. They depend on the box and Higgs amplitudes.

We find that the box contribution dominates the process except when the photon pair mass is close to the Higgs boson mass. Figure 3 shows the effect of the box-Higgs interference on the ratio F_2/F_1 as a function of Q around $m_H = 120$ GeV for a scalar or pseudoscalar Higgs boson. Away from $Q = m_H$ (by a few hundred MeV), we find $F_1 \gg F_2$, such that the additional term from linearly polarized gluons contributes at most 10% to the cross section but on average around 1% or less. However, near $Q = m_H$, where the Higgs contribution dominates, we find $F_1 \approx \pm F_2$. The ratio of the second to the first term in Eq. (16) then becomes approximately the ratio $\pm R$ of Fig. 2. Figure 3 suggests that a distinction between a scalar and a pseudoscalar Higgs boson is possible, if the experimental resolution of the photon pair mass Q is sufficiently good. Higgs bosons in extensions of the SM, which typically have larger widths, would require less fine Q binning. Also, for heavier Higgs bosons, other final states such as WW or ZZ production may allow for a better Q resolution. In any case, the Q -bin size around the Higgs boson mass is to be chosen as small as possible to maximize the effects caused by linearly polarized gluons.

We conclude that the effect of linearly polarized gluons on the Higgs transverse momentum distribution can, in principle, be used to determine the parity of the Higgs boson, provided $h_1^{\perp g}$ is of sufficient size. Of course, it could turn out that $h_1^{\perp g}$ is in reality smaller than in our model or that it exhibits nodes in x or p_T , complicating the

analysis. Our results thus provide additional motivation for experimental studies of $h_1^{\perp g}$ using different probes, such as dijet and heavy quark or photon pair production. We stress that perturbative gluon-radiation effects will alter the q_T distributions expected on the basis of our simple Gaussian model. Their inclusion will require merging our model with the soft-gluon resummation techniques described in Refs. [11,12,23,28,29]. This will also affect the eventual size of the contribution by linearly polarized gluons. A full study of this is needed.

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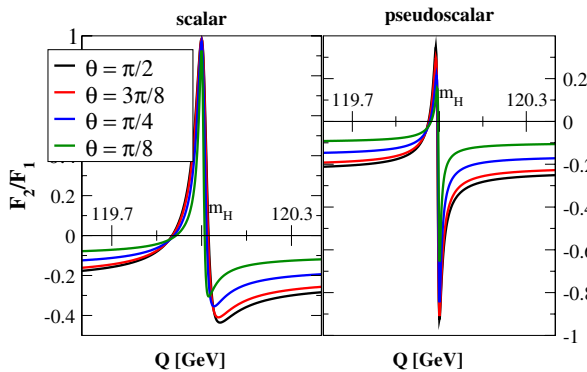


FIG. 3 (color online). Ratio F_2/F_1 as a function of pair mass squared in a region around $m_H = 120$ GeV for various angles θ .

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